

## **Supplemental Material on the Methodology and Results of the Study**

Here we discuss subsidiary analyses with the subset of the sample with schizophrenia, and details of our method of calculation of the average treatment effect.

### **Part A. Subsidiary Analyses of Persons with Schizophrenia**

As an additional check on our methods, we performed subsidiary analyses that were restricted to persons with schizophrenia (66% [112/170] of the mental health court participants and 7% [549/8,067] of the treatment as usual group). We performed intent-to-treat analyses that compared the mental health court participants and the treatment as usual group with schizophrenia from the time of enrollment to the end of the follow-up period, without distinguishing whether individuals successfully completed the mental health court program.

After controlling for propensity scores, demographic characteristics (e.g., sex and age), comorbid diagnoses, and number and type of charges during a 12-month baseline period, Cox proportional hazard models showed that mental health court participation predicted a longer time to any new charge ( $B = -0.38$ ,  $p < 0.01$ ) and longer time to a new violent charge ( $B = -0.058$ ,  $p < 0.05$ ).

Supplemental Figure 1 plots the average probability of a new charge as a function of months after entry to mental health court or treatment as usual based on the Cox model. (Supplemental Table 1 summarizes the plots at 6-month intervals and reports the 95% confidence intervals for the effect of mental health court participation on reducing the probability of a new charge.)

Supplemental Figure 1 shows that the effect of mental health court participation becomes more evident over time. By 18 months after entry, the cumulative probability of any new charge for

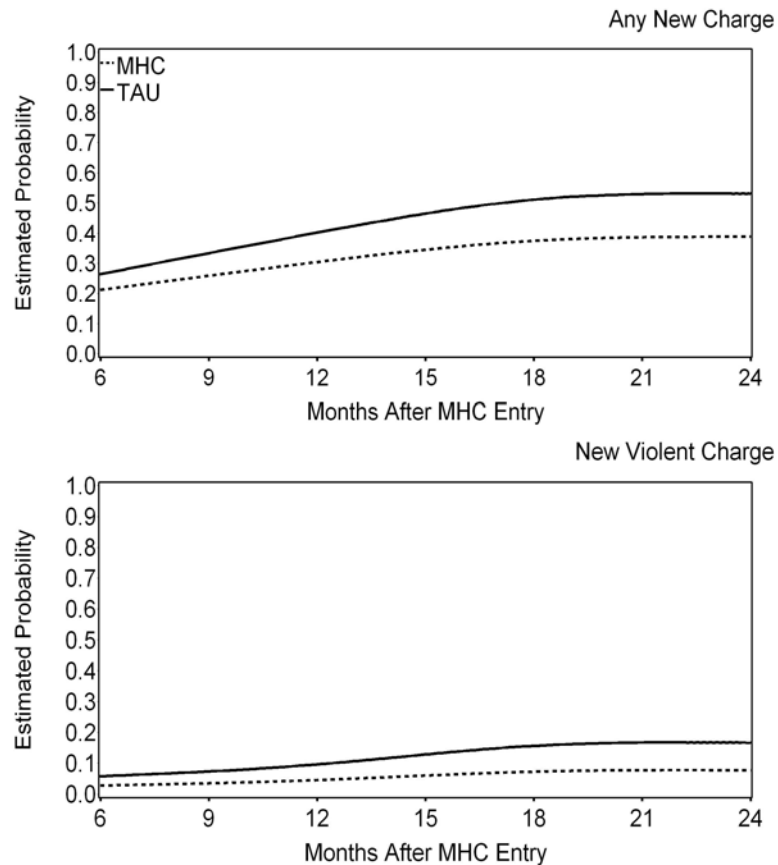
the mental health court participants and the treatment as usual group, respectively, was 0.38 and 0.51; at 18 months, the average reduction in the probability of a new charge due to mental health court participation was  $-0.14$  (95% CI =  $-0.16$  to  $-0.11$ ), which represents a 27% ( $0.14/0.51$ ) reduction. Similarly, Supplemental Figure 1 shows that the cumulative probability of a new violent charge, for mental health court participants and the treatment as usual group, respectively, was 0.07 and 0.16, at 18 months; the average effect of mental health court participation on reducing the probability of a new violent charge was  $-0.08$  (95% CI =  $-0.09$  to  $-0.08$ ), which represents a 50% ( $0.08/0.16$ ) reduction.

**Supplemental TABLE 1. Average Effect of Mental Health Court Participation on the Probability of a New Charge for Persons With Schizophrenia**

Months of Follow-Up	Mean (SD) Probability of New Charge		Average MHC Effect (SD): MHC – TAU	Standard Error of the Average MHC Effect	t	95% CI for the Average MHC Effect
	MHC <sup>a</sup>	TAU <sup>a</sup>				
<i>Months After Entry</i>						
<i>Any New Charge</i>						
6 Months	0.21 (0.20)	0.27 (0.07)	$-0.05$ (0.18)	0.023	$-2.28$	$-0.10$ , $-0.01$
12 Months	0.30 (0.25)	0.40 (0.09)	$-0.10$ (0.22)	0.011	$-9.13$	$-0.12$ , $-0.08$
18 Months	0.38 (0.28)	0.51 (0.09)	$-0.14$ (0.25)	0.010	$-13.88$	$-0.16$ , $-0.12$
24 Months	0.39 (0.28)	0.53 (0.09)	$-0.14$ (0.25)	0.010	$-14.69$	$-0.16$ , $-0.13$
<i>New Violent Charge</i>						
6 Months	0.03 (0.06)	0.06 (0.06)	$-0.03$ (0.05)	0.002	$-16.01$	$-0.03$ , $-0.03$
12 Months	0.05 (0.08)	0.10 (0.08)	$-0.05$ (0.07)	0.003	$-18.35$	$-0.06$ , $-0.05$
18 Months	0.07 (0.12)	0.16 (0.11)	$-0.08$ (0.10)	0.004	$-21.58$	$-0.09$ , $-0.08$
24 Months	0.08 (0.12)	0.17 (0.11)	$-0.09$ (0.11)	0.004	$-21.98$	$-0.10$ , $-0.08$

<sup>a</sup> MHC = mental health court; TAU = treatment as usual.

**Supplemental FIGURE 1. Estimated Cumulative Probability of a New Charge for Persons With Schizophrenia by Mental Health Court Status and Months After Entry<sup>a</sup>**



<sup>a</sup> MHC = mental health court; TAU = treatment as usual. The estimates are calculated from the propensity-weighted Cox proportional hazard model results.

In the aggregate, these results show similar average effects of mental health court participation on reduction in recidivism when analyses were restricted to persons with schizophrenia, as were evident in the more comprehensive analyses with the full study group that are reported in the print version of this manuscript.

## Part B: Method of Calculating the Average Treatment Effect

### B.1. Average Treatment Effects for the Cox proportional Hazards Model

Let us define  $MHC$  as an indicator variable for mental health court participation, where

$$MHC = \begin{cases} 0, & \text{if a TAU participant} \\ 1, & \text{if a MHC participant} \end{cases},$$

and let  $X$  be a  $k$ -dimensional vector of pretreatment variables. Assuming proportional hazards and a linear regression function for the pretreatment variables  $X$ , the logarithm of the hazard function for the Cox regression model is

$$\log(h(t, MHC, X)) = \alpha MHC + \sum_{j=1}^k \beta_j X_j + \sum_{j=1}^k \Delta_j X_j MHC$$

where the indicator variable  $MHC$ , each pretreatment variable  $X_j$ , and the product of  $MHC$  and each  $X_j$  are included as covariates.

For the subsample with the pretreatment variables  $X = x$ , with  $x$  being a particular set of values for the elements of  $X$ , the so-called *survival function* associated with the Cox model is defined by

$$S(t, x, MHC) = S_0(t) \exp\left(\alpha MHC + \sum_{j=1}^k \beta_j x_j + \sum_{j=1}^k \Delta_j x_j MHC\right),$$

and the failure function by:

$$F(t, x, MHC) = 1 - S(t, x, MHC) = 1 - S_0(t) \exp\left(\alpha MHC + \sum_{j=1}^k \beta_j x_j + \sum_{j=1}^k \Delta_j x_j MHC\right),$$

where  $S_0(t)$ , the baseline survival function, is given by  $-\log(S_0(t)) = H_0(t)$ , the baseline cumulative hazard function (1).

## Part B.2. Average Treatment Effect on the Failure Function

We are interested in the *average treatment effect* on the *failure function*, where the *average treatment effect* is taken to mean the amount by which the probability of reoffending as a function of time since baseline differs *on average* between two counterfactual scenarios—one where all individuals would be assigned to mental health court and the other where all individuals would be assigned to treatment as usual, conditional on all the above-mentioned confounding variables included in the Cox regression model. What would the expected treatment effect for an individual be if we were to manipulate the treatment condition for that individual from treatment as usual to mental health court, holding all  $x_j$ 's fixed? We describe these scenarios as counterfactual, since for those individuals in the sample who were actually in the mental health court group we do not have observations under the treatment as usual condition and, similarly, for those individuals who were actually in the treatment as usual group we do not have observations under the mental health court condition. This counterfactual construct is central to the treatment effect literature (2–6). Hence, the treatment effect for an individual can be formally expressed as

$$\begin{aligned}\tau_F(t, x_i, MHC) &= E\left\{ \left[ F(t, x_i, MHC_i, \alpha, \beta, \Delta) \mid MHC_i = 1 \right] - \left[ F(t, x_i, MHC_i, \alpha, \beta, \Delta) \mid MHC_i = 0 \right] \right\} \\ &= E\left[ F(t, x_i, MHC_i, \alpha, \beta, \Delta) \mid MHC_i = 1 \right] - E\left[ F(t, x_i, MHC_i, \alpha, \beta, \Delta) \mid MHC_i = 0 \right] \\ &= F_i^{MHC}(t, x, MHC, \alpha, \beta, \Delta) - F_i^{TAU}(t, x, MHC, \alpha, \beta, \Delta).\end{aligned}$$

Clearly,  $\tau_F(t, x_i, MHC)$  involves counterfactuals. However, it is also clear that  $\tau_F(t, x_i, MHC)$  represents the expected failure for an individual under the two different treatment conditions. Therefore, the *average treatment effect for individuals* is

$$\tau_F(t, x, MHC) = E\left[ F^{MHC}(t, x, MHC, \alpha, \beta, \Delta) - F^{TAU}(t, x, MHC, \alpha, \beta, \Delta) \right].$$

Following Terza (2) and Basu and Rathouz (3), once consistent estimates are obtained for the parameters of the Cox model ( $\hat{\alpha}$ ,  $\hat{\beta}_j$  and  $\hat{\Delta}_j$ ),  $\tau_F(t, x, MHC)$  can be consistently estimated by the sample average of the individual differences:

$$\hat{\tau}_F(t, x, MHC) = \frac{1}{n} \sum_{i=1}^n \left[ \hat{F}_i^{MHC}(t, x, MHC, \hat{\alpha}, \hat{\beta}, \hat{\Delta}) - \hat{F}_i^{TAU}(t, x, MHC, \hat{\alpha}, \hat{\beta}, \hat{\Delta}) \right],$$

which is the value of  $\tau_F(t, x, MHC)$  that minimizes the objective function

$$\sum_{i=1}^n \left\{ \left[ \hat{F}_i^{MHC}(t, x, MHC, \hat{\alpha}, \hat{\beta}, \hat{\Delta}) - \hat{F}_i^{TAU}(t, x, MHC, \hat{\alpha}, \hat{\beta}, \hat{\Delta}) \right] - \tau_F(t, x, MHC) \right\}^2.$$

The estimate  $\hat{\tau}_F(t, x, MHC)$  depends on the Cox model estimates  $\hat{\alpha}$ ,  $\hat{\beta}_j$  and  $\hat{\Delta}_j$ , and thus the usual calculated regression standard error for  $\hat{\tau}_F(t, x, MHC)$  is inconsistent and cannot be used. A consistent estimate of its standard error can be obtained by applying the method of Murphy and Topel (7) for two-step estimation to the objective function (see references 8 and 9 for further description of this method).

Since  $\tau_F(t, x, MHC)$  is the expected value of the failure function due to an experimental manipulation of treatment conditions for each individual, it can be characterized as representing the expected “causal” effect of treatment on the failure function. For complete details on Terza’s method, including proofs, see Terza (2). All results for Terza’s method hold when a propensity-weighted likelihood for the Cox regression model is used to obtain the estimates  $\hat{\alpha}$ ,  $\hat{\beta}_j$  and  $\hat{\Delta}_j$ .

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